Map/Reduce Affinity Propagation Clustering Algorithm

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Abstract—The Affinity Propagation (AP) is a clustering algorithm that does not require pre-set K cluster numbers. We improve the original AP to Map/Reduce Affinity Propagation (MRAP) implemented in Hadoop, a distribute cloud environment. The architecture of MRAP is divided to multiple mappers and one reducer in Hadoop. In the experiments, we compare the clustering result of the proposed MRAP with the K-means method. The experiment results support that the proposed MRAP method has good performance in terms of accuracy and Davies–Bouldin index value. Also, by applying the proposed MRAP method can reduce the number of iterations before convergence for the K-means method irrespective to the data dimensions.

Index Terms—affinity propagation, map/reduce, hadoop, K-means, clustering algorithm

I. INTRODUCTION

With the rapid speed of internet development, people get more focus on the Big Data issue. Big Data is a collection of data set so large that it becomes difficult to analyze. One of the common methods that help analyzing data is cluster analysis. The Affinity Propagation (AP) method [1], [2] is a clustering algorithm requires no pre-set number of clusters K. The AP method simultaneously considers all data points as the potential centers. The similarity $s(i,k)$ in AP indicates how well the data point with index k is suited to be the center for data point i. The AP finds the centers by passing two kinds of messages: “availability” and “responsibility”. The “availability” $a(i,k)$ which is passed between any two of data points shows the accumulated evidence for how appropriate it would be for point k to be chosen as point i’s center. The “responsibility” $r(i,k)$ which is passed between any two of data points shows the accumulated evidence for how well-suited the point i to be served as the point k. Fig. 1 shows how the availability and the responsibility work among data points.

Based on the original AP, there are many improvements to make AP more efficient. Wang et al. [3] extended the single-exemplar model to a multi-exemplar one to create a new Multi-Exemplar Affinity Propagation (MEAP) algorithm which can determine the number of exemplars in each cluster automatically. He et al. [4] presented a method which is called “Adaptive Affinity Propagation” to search the range of “preference” that AP needs then find a suitable value which can optimize the result of AP. The “preference” is important in AP to decide the result is good or not. A more suitable preference value makes the clusters assignment more reasonable.

Figure 1. The messages (“responsibility” $r(i,k)$ and “availability” $a(i,k)$ ) passing between any two points.

To adapt the Map/Reduce model, the proposed system of this work is built on top of the Apache Hadoop. The Apache Hadoop is an open-source software framework of the Map/Reduce model that provides an inexpensive way for processing big data to be seamlessly handled through multiple distributed computers [5]. The Map/Reduce applications are divided into many small fragments (every fragment is called mapper) to work then merge the results of all the small fragments in the reducer. Because the Map/Reduce model is parallel and distributed computing model, it is appropriate for the implementation of scalable clustering algorithms [6]. There are many differences need to be noticed between the Map/Reduce and the serial programming models to promise the Map/Reduce model can handle the reliability and data motion well [7]-[9].

In this work, we propose to improve the original Affinity Propagation (AP) method for cluster analysis to the Map/Reduce Affinity Propagation (MRAP) method in
Hadoop. The proposed MRAP method is a clustering algorithm for Map/Reduce model and it is scalable on multiple nodes for processing big data.

The main contributions of the proposed MRAP method are:

1. The MRAP method allows partitioning a single cluster analysis job into many small pieces on distribute processing nodes and to make the processing of big data more efficient and more scalable.

2. The MRAP method is self-regulating and thus requires no a priori knowledge of the characteristics of the input data. Hence the MRAP method is suitable for the Big Data environment.

3. The MRAP method can be the initialization of clustering algorithms that require a priori parameter settings such as the Map/Reduce K-means method.

The rest of this paper is organized as follows: In Section 2, we discuss the details of AP method and the proposed MRAP method and other algorithms that are used in experiments. After implementing the MRAP method, we test the result with running time, accuracy, and take the result of MRAP as the pre-cluster for K-means in Section 3. The results show that we get higher accuracy and less processing time than other comparing clustering algorithms in the Apache Mahout. In the end, we conclude this work and discuss the future work in Section 4.

II. ALGORITHM DESIGN

The AP is the kernel of our proposed algorithm. The AP is a clustering algorithm without the pre-known cluster number and the usual clustering algorithms are quite sensitive with selected initial centers. The AP classifies data by communicating data property between data points. Base on Affinity Propagation, we improve it to design MRAP in the Map/Reduce environment. We divide the original AP into two stages: the mapper stage and the reducer stage [10] for multiple computers. The architecture helps the AP works more efficiently and can handle larger dataset.

In this section, we first introduce how the AP works and discuss how to find a better preference value that the AP required. Second, we discuss how to improve the AP and discuss how to find a better preference value that the AP can handle larger datasets. There are three terminal conditions for AP: (1) a fixed number of iterations are passed (2) the changes of preferences are: 

\[ a(i,k) \leftarrow \min \left\{ 0, r(i,k) + \sum_{i' \in \mathbb{I}, i' \neq k} \max \{0, r(i',k) \} \right\} \]  

For \( k = i \), the responsibility \( r(k,k) \) is set to the input preference that point \( k \) be chosen as the center, \( s(k,k) \), minus the largest of the similarities between point \( i \) and all other candidate centers. But the self-availability \( (a(k,k)) \) is updated separately:

\[ a(k,k) \leftarrow \sum_{i' \in \mathbb{I}, i' \neq k} \max \{0, r(i',k) \} \]  

When updating the messages, it is important to avoid numerical oscillations. Each message is set to be \( \lambda \) multiply the value from the previous iteration plus \( 1 - \lambda \) multiply the prescribed update value, as shown in (5). The default damping value \( \lambda \) is 0.5.

\[ updated \text{ message} \leftarrow updated \text{Value} \cdot (1 - \lambda) + old \text{Value} \cdot \lambda \]  

where updatedValue means updated availability and responsibility; oldValue means availability and responsibility from previous iteration.

In later iterations, when some points are effectively assigned to other centers, their availabilities will drop below zero. For availability, only the positive portions of incoming responsibilities are added, because it is only necessary for a good center to represent some data points well, regardless of how poorly it represents other data points. There are three terminal conditions for AP: (1) a fixed number of iterations are passed (2) the changes of
messages fall below a threshold value and (3) the local decisions stay constant for some number of iterations. Fig. 2 shows how the AP works step by step.

For each point, combining the availabilities and responsibilities can identify its own center. For point $i$, the value of $k$ that maximizes $a(i,k) + r(i,k)$ either identifies point $i$ as a center if $k = i$, or identifies the data point that is the center for point $i$.

Each iteration of the AP consists of (i) updating all responsibilities given the availabilities, (ii) updating all availabilities given the responsibilities, and (iii) combining availabilities and responsibilities to monitor the center decisions and to decide termination or not.

Fig. 2 illustrates the AP for two-dimensional data points, where negative Euclidean distance (squared error) was used to measure similarity matrix. Through the exchange of availability and responsibility, shown as the blue lines during iteration, each point tries to decide its belonging to different clusters. The black arrow shows the final decision of clustering. The terminal condition is that the value of availability and responsibility does not vary through iteration or the floating values are below the threshold after a fixed number of iterations. The black arrow directed from point $i$ to point $k$ shows point $i$ belongs to cluster with center point $k$.

### B. Map/Reduce Affinity Propagation

We improve the AP in Map/Reduce environment to use multiple computers’ computing abilities more efficiently to handle larger data. Multiple mappers and two reducers are needed in this framework. The number of mappers is scalable. More mappers indicate that the data size for each mapper is smaller, but more mappers will make the communication between mappers more frequently. The framework of the proposed Map/Reduce Affinity Propagation (MRAP) is shown in Fig. 3.

First, the input data is preprocessed for initial similarity and preference values. The input data can be processed by multiple mappers at the same time. We divide the input data to small pieces randomly and stored both the source input data and the divided input data in the Hadoop Distributed File System (HDFS). The suitable preference value range can be decided through the method described by [4]:

**Step1. Initialize $s(k,k)$ to zero.**

$$s(k,k) = 0$$  \hspace{1cm} (6)

**Step2. Compute the maximal preference.**

$$P_{\text{max}} = \max\{s(i,k)\}$$  \hspace{1cm} (7)

**Step3. Compute the minimal preference.**

$$d_{\text{psim1}} = \max_{i\neq j}\left\{\sum_{k} s(i,k)\right\}$$  \hspace{1cm} (8)

$$d_{\text{psim2}} = \max_{i \neq j\neq k}\left\{\sum_{k} \max_{j} s(i,k),s(j,k)\right\}$$  \hspace{1cm} (9)

**Step4. Compute the minimal preference.**

$$P_{\text{min}} = d_{\text{psim1}} - d_{\text{psim2}}$$  \hspace{1cm} (10)

The range of preference value is from $P_{\text{min}}$ to $P_{\text{max}}$.

In the mapping stage, every mapper will get different divided data from the HDFS and will perform the AP on their own data. During the AP, each mapper uses its own similarity matrix and preference values. After the AP, each mapper gets the cluster centers and cluster points for its own data. Each mapper has its own key to transmit its result to the next reducing stage. If point $i$’s center is point $k$, the transmitted data tuple is $<key, i, k>$. In the Map/Reduce environment, all parameters transmit between a mapper and a reducer (or a mapper and another mapper, or a reducer and another reducer) have to be the form of $<key, value>$. The Map/Reduce unit will collect the values with the same key and process the values at the same time.

There are two reasons that each mapper should perform the AP independently with its own data: (1) in the AP, there are about hundreds of iterations needed. If we exchange the information for every iteration, a huge communication cost is expected in the map/reduce environment. (2) Every mapper is isolated in processing, which is restricted by the architecture to transfer data among mappers.

The reduce stage is composed of two parts: classify points and calculate the center points. Reducer A
classifies the clustered points and sends the result to
reducer B to calculate the centers of clusters.

In reducer A, clustered points and their own centers are
collected from the results of mappers. If the distance
between two centers is less than the threshold, the points
that are originally in two clusters will be combined into
one cluster. Through experiments, the recommended
threshold value is set to preference*0.5. The threshold
value can be adjusted with different input data sets. The
result is that points from different mappers with
neighboring centers will be classified into the same
cluster. The points that are far away from other data
points will be classified as isolated points. There are two
conditions that a point will be classified as isolated points:
(1) if a cluster have few points and (2) the cluster’s center
is very far away from other clusters. In the end of reducer
A, the points that are in the same cluster will be sent to
reducer B by the same key.

In reducer B, there may be multiple centers in a cluster.
To decide the true centers of clusters, we employ the
centroid of centers from reducer A. If there are K centers
from reducer A, the centroid is decided as in (11).

\[
\text{Centroid} = \frac{C_1 + C_2 + C_3 + \ldots + C_k}{K}
\]  

After combining clusters, the centers of clusters are
decided and the points of those combined clusters will be
renumbered. Different cluster centers and their own
clustered points are set with unique keys and then output.
The output results are sets of clustered points and their
corresponding cluster centers.

![Figure 4. The processing stages of MapReduce affinity propagation.](image)

Fig. 4 shows how the MRAP works: before the input to
be processed, the MRAP divides data randomly and
computes the similarity in the preprocessing stage. In the
map stage, every mapper gets a part of divided data and
performs AP independently. In the map stage of Fig. 4,
color dots with black outlines denote the cluster centers
after affinity propagation. Then the mappers deliver their
own clustering results to the next stage. The reducer
combines the clusters from the map stage and calculates
the new cluster centers after combining neighboring
clusters. During the process of calculating the new cluster
centers, the reducer removes points that are far away
from any of the clusters. In the end, the MRAP outputs
the details of clusters including the final cluster centers
and every point in each cluster.

III. EXPERIMENTS

In the following experiments, the proposed MRAP is
compared with the Map/Reduce K-means algorithm,
which is included in the Apache Mahout Classification
package. The experiments are divides into four sections:
(1) running time, (2) accuracy, and (3) using the
clustering results of the MRAP as the initial points for the
K-means algorithm and compare to other initial methods
for the K-means algorithm. We chose two datasets (iris
and wine quality) from the UC Irvine Machine Learning
Repository [11] and The Yale Face Database
[12]. Experiment environments as follow:

- Master (CPU: Intel® Core™2 Quad Processor
  Q6600 (8M Cache, 2.40 GHz, 1066 MHz FSB);
  RAM: DDR2-800 2G * 2)
- Node1 for NameNode and JobTracker
- Slave (CPU: Intel® Core™2 Quad Processor
  Q6600 (8M Cache, 2.40 GHz, 1066 MHz FSB);
  RAM: DDR2-800 2G * 2)
- Node2~9 for DataNode and TaskTracker

1) Running time test

In this experiment, we focus on the processing time
with different data dimensions and the number of data
points is fixed to 5000. We chose the Canopy method as
the comparing algorithm because similar to the MRAP,
the a priori knowledge of the number of clusters is not
required for the Canopy method.

![Figure 5. The result of running time experiment.](image)

The dimension of input data varies from 4 to 1200. By
employing the MRAP, the running time is about 5.5
minutes and does not increase when the dimensionality
of data increases. Comparing to the Canopy method, the
running time increases almost linearly when the
dimensionality increases. While applying the Canopy
method, we start getting the “Java heap error” when the
dimension is increased to about 400. An as a result, the
experiment cannot be completed beyond 400 dimensions.
To try to conquer the error, we increase the RAM for
each salve node from 1G to 4G, but the error persists
disregarding the additional memory space. Fig. 5 shows
the running time of the MRAP and the Canopy methods.
The solid lines show the actual observed data, the dotted
line is an interpolation because the experiments cannot be completed with “Java heap error”.

2) Accuracy test

The Canopy method as the initialization of the Map/Reduce K-means algorithm is chosen for the comparison study here. The accuracy which includes the precision rate and the recall rate of the MRAP and the Canopy method is presented in this section.

The dimension of the Iris dataset is 4. The T1 and T2 values of the Canopy method are set to the optimal values through many trials. As shown in Table I, the MRAP and the Canopy initialized Map/Reduce K-means method produce similar accuracy when the dimensionality is low.

<table>
<thead>
<tr>
<th>Cluster</th>
<th>Precision</th>
<th>Recall</th>
<th>Precision</th>
<th>Recall</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cluster1</td>
<td>0.69</td>
<td>0.98</td>
<td>0.723077</td>
<td>0.94</td>
</tr>
<tr>
<td>Cluster2</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Cluster3</td>
<td>0.97</td>
<td>0.56</td>
<td>0.914286</td>
<td>0.64</td>
</tr>
<tr>
<td>Average</td>
<td>0.8867</td>
<td>0.84667</td>
<td>0.87667</td>
<td>0.86</td>
</tr>
</tbody>
</table>

The dimension of the Wine quality dataset is 11. The T1 and T2 values of the Canopy method are not set to the optimal values because it is hard to decide the suitable T1, T2 when the dimensionality is increasing. When the T1 and T2 values deviate from the prospective ranges, data points will be assigned to only specific clusters, as shown in Table II. The result is that the precision rate and the recall rate decrease significantly. The MRAP method produces more stable clustering output than the Canopy initialized Map/Reduce K-means when the data dimensionality increases.

<table>
<thead>
<tr>
<th>Cluster</th>
<th>Precision</th>
<th>Recall</th>
<th>Precision</th>
<th>Recall</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cluster1</td>
<td>0.75</td>
<td>0.1472</td>
<td>0.0615</td>
<td>1</td>
</tr>
<tr>
<td>Cluster2</td>
<td>0.4665</td>
<td>0.1584</td>
<td>0.0745</td>
<td>0.1123</td>
</tr>
<tr>
<td>Cluster3</td>
<td>0.4474</td>
<td>0.2253</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Cluster4</td>
<td>0.1823</td>
<td>0.3643</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Cluster5</td>
<td>0.0543</td>
<td>0.4629</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Average</td>
<td>0.466</td>
<td>0.267</td>
<td>0.026</td>
<td>0.22</td>
</tr>
</tbody>
</table>

To sum up, the proposed MRAP method and the Canopy initialized Map/Reduce K-means method have similar clustering accuracy when the data dimensionality is low and with simpler data distributions. When the data dimensionality increases, the data distributions tend to be more complex. However, the prospective T1 and T2 parameter values in the Canopy method are increasingly more difficult to find as the dimensionality increases. Even though we can get fair T1 and T2 values for the Canopy initialized Map/Reduce K-means method, the clustering accuracy is lower than the proposed MRAP method.

3) K-means initialization test

The following experiments try to decide which initialization algorithm can reduce the number of iterations before convergence for the Map/Reduce K-means method provided by the Apache Mahout package. Three algorithms are chosen in this experiment: the proposed MRAP method, the Canopy method, and the random seed method, where the latter two methods are provided by the Apache Mahout clustering package. Each method is repeated 10 times for different datasets in the experiments.

The Fig. 6 shows that the numbers of iterations before convergence for the Map/Reduce K-means method initialized by the Canopy method is generally less than initialized by the MRAP method and the random seed method. But the average clustering precision of the Canopy method (0.026) is much lower than the MRAP method (0.466), as discussed in the previous section.

The Fig. 7 shows the numbers of iterations before convergence for the Map/Reduce K-means method with the Iris datasets. Fig. 7 shows that the MRAP initialized Map/Reduce K-means can help to reduce the numbers of iterations before convergence significantly. The random seed method is generally requires higher number of iterations.

The Fig. 8 shows the numbers of iterations before convergence for the Map/Reduce K-means method with the Face dataset, which is 1200 in dimensions. In Section 3.1, we discuss that the Canopy initialized Map/Reduce K-means method cannot work in high dimensional data space. So in this experiment we only compare the proposed MRAP method with the random seed method. The results shown in Fig. 8 suggest that the proposed MRAP method can still reduce the number of iterations for the Map/Reduce K-means method in extreme high
dimensional data space. From the experiments in this section, the proposed MRAP method can reduce the number of iterations before convergence for the Map/Reduce K-means method irrespective to the data dimensions.

However, there are still several problems need to be solved in the future work. First, if it is possible to transfer data between mappers during the cluster processing, it can make the MRAP more efficient. The Map/Reduce 2.0 [13] architecture under developing will allow information transfer between mappers and hence can further improve the performance of the proposed MRAP in the future. Second, for the threshold of combining the clusters from mappers, we can try to automatically decide the threshold by clusters’ variance, which may help to improve the accuracy of the MRAP.

ACKNOWLEDGMENT

This work was partially supported by the National Science Council, Taiwan, under the Grants No. NSC102-2221-E-011-134, NSC102-2221-E-211-012.

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