An Analog Circuit Diagnosis Method Based on Adaptive-Kernel ICA

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Abstract—An analog circuit fault diagnosis method based on an adaptive kernel function is presented. The adaptive kernel function is built by using the linear properties of the kernel functions. There are three steps for analog circuit diagnosis: preprocessing, feature extraction and faults classifying. The data is de-noised and centralized by preprocessing step firstly. Then a feature extraction method based on AMK-ICA technology is presented to lower the dimension of the data. Finally, the support vector machine is used to identify the fault mode of the circuit under test. Experimental study shows that the method can effectively improve the samples training time, test time and identification precision compared with the main reference cited in this paper.

Index Terms—analog circuit, fault diagnosis, independent component analysis, support vector machine

I. INTRODUCTION

With the rapid development of modern electronic industry, the analog and digital hybrid integrated circuit develops very fast. Eighty percent of the faults are the analog circuit faults, so the reliability of the analog circuit almost decides the reliability of the whole electronic systems [1], [2]. Analog circuit fault diagnosis has decades of research background. In 1985, J. W. Bandler and A. E. Salama illustrated the diagnosis of analog circuit fault in detail [3], henceforward the diagnosis of analog circuit is more popular. Now the research achievements of analog circuit fault diagnosis is fruitful [4]-[7]. There are many circuit fault diagnosis methods [4]-[7]. But these methods need to be improved before they can take into practice for the complexity and high computational time [4], without considering the fault tolerance [5], the need of exploring high performance algorithm [6], [7].

Independent component analysis (ICA) has attracted much attention since it proposed [8]-[10], and it has been applied in many fields, such as voice recognition field [8], [11], image recognition field [9] and data extraction field [10]. Feature extraction is of great importance in analog circuit diagnosis. The documents [12], [13] verified that kernel function can be used to extract data feature, but a single kernel function can’t adjust the feature extraction strategy self-adaptively according to the system requirements [14]. Considering the need of analog circuit diagnosis, an adaptive kernel independent component analysis (AMK-ICA) is presented and it is verified by support vector machine.

The material in this paper is arranged in the following order: In Section 2, we briefly discuss the basic theory of kernel and mixed kernel function. Section 3 studies the system of analog fault diagnosis and procedure based on AMK-ICA-SVM. Section 4 discusses example circuits and application of the proposed method. Section 5 gives the analysis and summary of the system.

II. THE ADAPTIVE KERNEL FUNCTION THEORY

There are 3 popular kernel functions [15]:

Polynomial kernel function
\[ K(x, y) = (1 + (x \cdot y))^d, \quad d = 1, 2, \ldots \]
\[ (1) \]

Gauss RBF nuclear function
\[ K(x, y) = \exp\left(-\frac{1}{\delta^2} \|x - y\|^2\right) \]
\[ (2) \]

Perceptron kernel function
\[ K(x, y) = \tanh(\nu (x \cdot y) + c) \]
\[ (3) \]

\(d, \sigma, \nu, c\): real constant parameters

Figure 1. RBF kernel function
Fig. 1 and Fig. 2 represent Gauss RBF nuclear function and Perceptron kernel function respectively. The figures show that when $\sigma$ is smaller, the curve is shaper and the function’s learning ability is better. Comparing Gaussian RBF with Perceptron kernel function, we discover that Gaussian RBF kernel function has a stronger learning ability and weaker generalization. On the contrary, the Perceptron kernel function has stronger generalization and learning ability.

The kernel functions have the following properties:

$$K(x, y) = \sum_{i=1}^{n} m_i K_i(x, y)$$
$$\sum_{i=1}^{n} m_i = 1, i = 1, 2...n$$

$K_i(x, y)$: the i-th a kernel function

where $m_i$ is an adjust parameter to combine hybrid kernel function and $K_i(x, y)$ is used to construct the hybrid kernel function. Considering the requirements of generalization and learning abilities in the system, we select Gaussian kernel function with Perceptron kernel function to construct an adaptive hybrid kernel function.

$$K(x, y) = \lambda \exp\left(\frac{(x-y)^2}{\sigma^2}\right) + (1-\lambda) \tanh(v(x \cdot y))$$

where the parameters of combination of hybrid kernel function $\lambda$, the steep coefficient of kernel function $\sigma$, and $v$ is a constant coefficient. When $\lambda$ takes large values and $\sigma$ takes small values, learning ability is stronger and generalization is weaker; and vice versa. In general for the greater change of the data we demand that learning ability is stronger in the system and for the flat change of the data we demand that generalization is stronger.

The Euclidean distance [16] reflects the true distance between two vectors and also the similarity between the two signals. Therefore, this article considers the sample Euclidean distance as the basis of adaptive adjusting the combining parameters. Suppose there are $M$ test vector samples, $z_i$ is the Euclidean distance between vector $x_i$ and vector $x_j (x \neq j)$. Let $z_{\text{max}} = \max(z_i)$, $z_{\text{min}} = \min(z_i)$, $z = [z_{12}, z_{13}, ..., z_{(M-1)M}]$, $i \neq j$. The parameters of combination of hybrid kernel function $\lambda$ is determined by the following equation:

$$\lambda = \frac{E[z]}{z_{\text{max}} - z_{\text{min}}}$$

where $E[z]$ represents the expectation value of vector $z$. So hybrid kernel function according to the data fluctuation in the samples adjusts adaptively the complex coefficient of hybrid kernel function.

### III. ANALOG CIRCUIT FAULT DIAGNOSIS BASED ON THE MIXED KERNEL FUNCTION

The basic principle of AMK-ICA is shown in the following Fig. 3. $S = [s_1(t), s_2(t), ..., s_n(t)]$ is the unknown source signals of the m-dimensional that the respective components of $S$ are mutually independent, and only have a component is Gaussian distribution. $A$ is the unknown hybrid matrix, $X$ is the observed signals, $W$ is the demixing matrix and $Y$ is the demixing signals.

![The principle of AMK-ICA](image)

The basic idea of AMK-ICA is to build the adaptive kernel function $K(x, y)$ by using demixing $Y$ and the observed signal $X$, so as to realize the adjustment of the demixing matrix $W$. That is to say:

$$Y = WX$$

And

$$X = AS$$

Demixing matrix $W$ and the unknown hybrid matrix satisfy $WA=I$, which $I$ is the unit matrix.

This means that we must firstly solve the demixing matrix $W$. Research in the document [17], [18] shows that the key of AMK-ICA is to find a direction $W^TX (Y = W^TX)$ so as to acquire the greatest nongaussian direction. As is concluded in the information theory: in all the variance of random variables, the Gaussian variable has a maximum entropy, and thus the maximizing the negative entropy $N_e(W^TX)$ can be used as a search for the direction of the maximum nongaussian objective function [18].

The detailed algorithms are given below:

1. Centralize the observation data, make its mean value be zero.
2. Whiten the data, $X \rightarrow Z$, $Z$ is for whiten vector.
3. Choose an initial vector randomly.
4. Build the Newton iterative equation based on negative entropy maximization.


\[ W_p = E\{ZK(W^TW)\} - E\{ZK(W^T Z)\} W, \quad K(\cdot) \]

is the constructed adaptive hybrid function in Section 2.

5. The iterative equation: \( W_p = W_p - \sum_{j=1}^{\infty} (W^TW_j)W_j \).

6. Normalize: \( W_p = W_p / \|W_p\| \).

7. If \( W_p \) is not converged, return to step 5. Until \( \sum_{j=1}^{\infty} (W^TW_j)W_j \) is near zero, the \( W_p \) gets a final value.

IV. EXPERIMENTAL RESEARCH

A. The Model of Measured Circuit and Flow Chart of AMK-ICA-SVM Experiment

Considering one typical diagnosis circuits: the Salley-Key linear band-pass filter. The data acquisition process is shown in Fig. 4.

![Figure 4. The model of testing circuit diagnosis](image)

The measured circuit diagnosis model is consist of oscilloscope (DS1102E), experiment box (ZXEET232), the chip of data acquisition (JCJ716AI) and computer (Lenovo s525).

After using data acquisition chip to get the original data, then we use the AMK-ICA-SVM method to process them. The specific process is shown in the below Fig. 5.

![Figure 5. The experiment flow chart of AMK-ICA-SVM](image)

The AMK-ICA-SVM in the Fig. 5 is divided into four modules, namely the original data classification module, AMK-ICA feature extraction module, training SVM module and the out module. Firstly we divide the original data into two categories—the training sample and testing samples. Then we give the data to training and testing SVM after AMK-ICA processing, and the resulting data is the accuracy classification at last.

B. Linear Circuit Diagnosis—Salley-Key Band-Pass Filter

We use the above method to test Salley-key band-pass filter, which are shown in Fig. 6.

![Figure 6. Salley-Key band-pass filter circuit](image)

The components on the target value in the Fig. 6 are standard under the parameter of normal working state, and the center frequency of the circuit is 25KHZ. The experimental part of analog circuit soft fault in the literature [19] proposes the method of the minimum detectable fault size (MDFS). Based on the comprehensive consideration of MDFS method according to the specific circuit, we suppose the circuit occurs to soft fault that the values of the circuit components deviate 10% from the normal value. The types of soft fault are shown in below Table I.

<table>
<thead>
<tr>
<th>The type of fault</th>
<th>The code of fault</th>
<th>The value of soft fault</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1↑</td>
<td>F1</td>
<td>0.9 0.81 0.73K</td>
</tr>
<tr>
<td>R1↑</td>
<td>F2</td>
<td>1.1 1.21 1.33K</td>
</tr>
<tr>
<td>R2↑</td>
<td>F3</td>
<td>2.7 2.43 2.18K</td>
</tr>
<tr>
<td>R2↑</td>
<td>F4</td>
<td>3.3 3.36 3.99K</td>
</tr>
<tr>
<td>R3↑</td>
<td>F5</td>
<td>1.8 1.62 1.45K</td>
</tr>
<tr>
<td>R3↑</td>
<td>F6</td>
<td>2.2 2.42 2.66K</td>
</tr>
<tr>
<td>R4↑</td>
<td>F7</td>
<td>3.6 3.24 2.91K</td>
</tr>
<tr>
<td>R4↑</td>
<td>F8</td>
<td>4.4 4.84 5.32K</td>
</tr>
<tr>
<td>R5↑</td>
<td>F9</td>
<td>3.6 3.24 2.91K</td>
</tr>
<tr>
<td>R5↑</td>
<td>F10</td>
<td>4.4 4.84 5.32K</td>
</tr>
<tr>
<td>C1↓</td>
<td>F11</td>
<td>4.5 4.05 3.64K</td>
</tr>
<tr>
<td>C1↓</td>
<td>F12</td>
<td>5.5 6.05 6.65K</td>
</tr>
<tr>
<td>C2↓</td>
<td>F13</td>
<td>4.5 4.05 3.64K</td>
</tr>
<tr>
<td>C2↓</td>
<td>F14</td>
<td>5.5 6.05 6.65K</td>
</tr>
</tbody>
</table>

The Salley-key band-pass filter circuit is constructed with experiment box, and the test is done under various kinds of soft faults of the circuit, then some data is obtained by data acquisition chip; finally we use the method of AMK-ICA-SVM to extract 200 characteristics of the samples in the original data, which can be divided into two parts, 110 samples are used as training SVM, the other 90 samples are used as test SVM.

The output of AMK-ICA are shown in the below Table II, which the column represents the fault types of the Salley-key band-pass filter circuit and the row represents the part of the eigenvalues based on AMK-ICA to extract the circuit.
The Gaussian kernel function, multi-layer perceptron kernel function and adaptive hybrid kernel function are shown respectively in the following Table III, which adopt the SVM of the one-against-one training and multiple classification in the fault diagnosis of analog circuit.

<table>
<thead>
<tr>
<th>The kinds of kernel function</th>
<th>The number of training samples</th>
<th>The training time(s)</th>
<th>The testing time(s)</th>
<th>The accuracy of classification</th>
</tr>
</thead>
<tbody>
<tr>
<td>The gaussian</td>
<td>110</td>
<td>2.51</td>
<td>0.83</td>
<td>96.29%</td>
</tr>
<tr>
<td>The perceptron</td>
<td>110</td>
<td>5.21</td>
<td>1.65</td>
<td>94.14%</td>
</tr>
<tr>
<td>Adaptive hybrid</td>
<td>110</td>
<td>1.51</td>
<td>0.67</td>
<td>97.75%</td>
</tr>
</tbody>
</table>

The result of classification in the Salley-key filter circuit based on the SVM of adaptive hybrid kernel function in the following Fig. 7, which the one horizontal axis represents the combination of the kernel function parameters $\lambda$, the another horizontal axis represents the steep coefficient $\delta$, and the vertical axis represents the classification accuracy.

![Parameter selection result of SVC(3D VIEW)(Adaptive kernel function)](image)

**Figure 7.** Salley-Key filter circuit based on adaptive hybrid kernel function of SVM classification figure

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**REFERENCES**


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